# Effect of Temperature on Interatomic Distances in Pyroelectric $\alpha_{\text {- }} \mathrm{LiIO}_{3}$ 

By E. Coquet and J. M. Crettez<br>Laboratoire d'Optique du Réseau Cristallin, Faculté des Sciences, Dijon, France<br>J. Pannetier and J. Bouillot<br>Institut Laue-Langevin, 156X, 38042 Grenoble, France<br>and J. C. Damien<br>Université des Sciences et Techniques de Lille, 59655 Villeneuve d'Asq, France

(Received 14 May 1982; accepted 8 March 1983)


#### Abstract

The crystal structure of $\alpha-\mathrm{LiIO}_{3}$ (space group $\mathrm{Pb}_{3}$ ) has been refined from neutron and X-ray diffraction data at different temperatures between room temperature and 525 K . The Li atom is well located even at temperatures close to the $\alpha \rightarrow \gamma$ phase transition and its thermal parameters do not exhibit any anomalous behaviour. The thermal expansion is analysed in terms of $\mathrm{IO}_{3}$-group rotations and expansion of $\mathrm{LiO}_{6}$ octahedra; the role of the iodine lone pair in the packing of iodate structures is discussed. The spontaneous polarization is calculated on the basis of a simple pointcharge model and the calculated pyroelectric coefficient $P_{3}$ is found to be in fair agreement with the experimental value.


## Introduction

Although the room-temperature (RT) structure of $\alpha-\mathrm{LiIO}_{3}$ has been extensively studied by X-ray (Rosenzweig \& Morosin, 1966; de Boer, van Bolhuis, Olthof-Hazekamp \& Vos, 1966) and neutron diffraction (Emiraliev, Kocharov, Yamzin \& Lyubimtsev, 1976), little is known about its modifications at higher temperatures. Among the pecularities which are not yet understood are the structural mechanism of the $\mathrm{Li}^{+}$ conduction and the differences in the sequence of phase transitions between single crystals and powders: indeed, single crystals usually transform directly from $\alpha$ to $\beta$ - $\mathrm{LiIO}_{3}$ whereas powdered samples transform from $\alpha$ - to $\beta$ - $\mathrm{LiIO}_{3}$ through an intermediate, orthorhombic $\gamma-\mathrm{LiIO}_{3}$ whose structure is still unknown.

As part of an extensive program of research on the structures and physical properties of the three phases of lithium iodate, we report in this paper a structural investigation of $\alpha-\mathrm{LiIO}_{3}$ at four different temperatures (RT, 373, 475 and 525 K ). Consequently, the thermal

0108-7681/83/040408-06\$01.50
expansion, the lone pair and the pyroelectric coefficient are also discussed.

## Experimental

The $\alpha$ - $\mathrm{LiIO}_{3}$ single crystal used for neutron diffraction (size $2 \times 2 \times 6 \mathrm{~mm}$ ) was grown by slow evaporation of an aqueous solution of ${ }^{7} \mathrm{LiIO}_{3}$ at $\mathrm{pH}=6$ and $T=318$ K . The crystals used for the X-ray diffraction experiment were grown in a similar way from a natural lithium iodate solution (size $0.2 \times 0.2 \times 0.45 \mathrm{~mm}$ ); powders were prepared from these crystals. All crystals show the characteristic morphology previously described by Rosenzweig \& Morosin (1966).

The powder diffraction patterns were recorded on the D1A high-resolution diffractometer of the ILL with $\lambda=1.3885$ (3) and 1.9066 (3) $\AA$, the wavelength being calibrated with a Ni powder standard ( $a=3.5238 \AA$ ). The powdered sample was inserted in a cylindrical vanadium container ( $\varnothing=15 \mathrm{~mm}$ ). The heating device was a conventional furnace with a vanadium heater working under low helium pressure. The temperature was measured with a $\mathrm{Ni}-\mathrm{Cr}$ thermocouple in contact with the sample holder. Data were collected from $2 \theta=$ $10^{\circ}$ to $160^{\circ}$ in steps of $0.05^{\circ}$. Measurement times were about $15 \mathrm{~s}(1.91 \AA)$ and $30 \mathrm{~s}(1.39 \AA)$ per step. The data of the 10 counters were summed using a conventional ILL Program (Hewat, 1978). The RIETVELD program (Rietveld, 1969) as modified by Hewat (1973) was used for the profile-fitting structure refinement. The thermal parameters were corrected for absorption ( $\mu R=0.42$ ) according to Hewat (1979) (correction to be divided by 2 ) ( $\mu=0.55 \mathrm{~cm}^{-1}$ ).

Single-crystal neutron experiments were performed at room temperature, 373 and 475 K on the D9 four-circle diffractometer located on the hot source of the ILL. Data were collected with a wavelength of 0.5499 (3) $\AA$. The crystal was mounted in a small © 1983 International Union of Crystallography
aluminium furnace (kindly provided by Dr G. Heger, KFZ, Karlsruhe) which allows the temperature to vary in the range RT to 523 K . Totals of 526 (RT), 465 ( 373 K ) and $700(475 \mathrm{~K}$ ) reflections with $0<h, k, l \leq$ 10 were measured by $\omega$ scans to $\sin \theta / \lambda=1 \cdot 17 \AA^{-1}$. The raw data were reduced to $F^{2}$ values by the method of Lehmann \& Larsen (1979); no attempt was made to correct for absorption ( $\mu=0.057 \mathrm{~cm}^{-1}$ ). The data were then averaged so that the final refinements in space group $P 6_{3}\left(C_{6}^{6}\right)$ are based on about 400 independent reflections with $F / \sigma(F)>3$. The scattering lengths used for the refinement of neutron data were taken from Koester \& Rauch (1981): $b(\mathrm{Li})=$ $-2.03, b\left({ }^{7} \mathrm{Li}\right)=-2.197, b(\mathrm{I})=5.28$ and $b(\mathrm{O})=5.805$ fm.

Single-crystal X-ray measurements were performed at 525 K with an automatic four-circle diffractometer (Philips PW 1100) using monochromatized Mo $K \alpha$ radiation $(\lambda=0.7107 \AA$ ). The sample was heated by a temperature-controlled nitrogen gas flow device. The temperature calibration was made using the transition temperature of $\mathrm{NaNO}_{3}(T=549 \mathrm{~K}$ ) and gives an accuracy certainly better than $\pm 3 \mathrm{~K}$ (mainly due to thermal gradient). Data ( $0<h, k \leq 9,0<l \leq 8$ ) were collected by the $\omega-2 \theta$ scan method up to $\sin \theta / \lambda=$ $0.96 \AA^{-1}$. Reflections are scanned with a speed of 0.03 $\mathrm{s}^{-1}$; a fixed scan width of $2^{\circ}$ was used. A total of 1081 reflections were collected and corrected for Lorentzpolarization. An attenuation filter was used for the most intense reflections. The data were subsequently corrected for absorption ( $\mu=115 \mathrm{~cm}^{-1}$ ) using a local version of the grid method (Coppens, Leiserowitz \& Rabinovich, 1965). After symmetry-equivalent reflections were averaged, 318 independent reflections were judged to be observed by the criterion $F>\sigma \sigma(F)$. The scattering factors and anomalous-dispersion corrections for all atoms ( $\mathrm{Li}^{+}, \mathrm{I}, \mathrm{O}^{-}$) were taken from International Tables for X-ray Crystallography (1974).

All structure refinements were performed with the computer program SHELX (Sheldrick, 1976). Anisotropic thermal parameters were used except for Li which was not located accurately enough by X-rays at that temperature. In the final refinement cycles, the weighting scheme was $w=12 /\left[\sigma^{2}(F)+0.000135 F^{2}\right]$.

## Crystal data and structure refinements

Table 1 gives the results of structure refinements at different temperatures and wavelengths under the conditions defined in Experimental.* The results of Rosenzweig \& Morosin (1966), de Boer et al. (1966), and Emiraliev et al. (1976) are also reported. The $\alpha$ - $\mathrm{LiO}_{3}$ space group is $P 6_{3}$, with two formula units in the cell. All relative atomic positions are given in the same system of coordinates, i.e. Li in $[0,0, z(\mathrm{Li})]$, I in $\left(\frac{2}{3}, \frac{1}{3}, 0\right), \mathrm{O}$ in $(x, y, z)$. Such a configuration corresponds to an $L$-type crystal where the $z>0$ axis is chosen along the - $\mathbf{c}$ direction of the absolute configuration ( Li , 1981). Standard deviations are given in parentheses and refer to the last digit. The equivalent isotropic thermal parameters are reported in Table 1 as $B_{\text {eq }}=$ $8 \pi^{2}\left(2 U_{11}+U_{33}\right) / 3$ for Li and I , and $B_{\text {eq }}=8 \pi^{2}\left[4\left(U_{11}+\right.\right.$ $\left.\left.U_{22}-U_{12}\right) / 3+U_{33}\right] / 3$ for O . The results of different authors are in good agreement at room temperature.

[^0]Table 1. $\alpha$ - $\mathrm{LiIO}_{3}$ cell parameters, relative atomic positions $\left(\times 10^{4}\right)$ and equivalent isotropic thermal parameters $\left(\AA^{2}\right)$ calculated from refined anisotropic thermal parameters

|  | Rosenzweig \& Morosin | de Boer et al. | Emiraliev et al. |  |  | This work |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Method ${ }^{*}$ | $X$ | X | $N P$ | $N P$ | $N$ | $N$ | $N$ | $X$ |
| $T$ (K) | RT | RT | RT | RT | RT | 373 | 475 | 525 |
| $\lambda(\mathrm{A})$ | 0.7107 | 0.70926 | 1.24 | 1.3885 | 0.5499 | 0.5499 | 0.5499 | 0.7107 |
| $a(\AA)$ $c(\AA)$ | $5.4815(3)$ $5.1709(4)$ | $5.478(3)$ $5.170(2)$ | 5.48 5.17 | $5.4851(1)$ $5.1752(1)$ | $5.477(3)$ $5.170(2)$ | $5.489(3)$ $5.193(2)$ | $5.507(2)$ $5.219(2)$ | $5.516(3)$ $5.236(2)$ |
| $z(\mathrm{Li})$ | 8907 (123) | 9110 (50) | 9270 (67) | 9244 (14) | 9231 (10) | 9195 (15) | 9202 (12) | 9034 (90) |
| $x(0)$ | 3440 (20) | 3425 (8) | 3437 (13) | 3431 (2) | 3418 (1) | 3422 (2) | 3425 (2) | 3428 (8) |
| $y(\mathrm{O})$ | 2504 (21) | 2485 (8) | 2470 (13) | 2477 (2) | 2471 (2) | 2462 (3) | 2449 (2) | 2413 (13) |
| $z$ (O) | 1698 (20) | 1652 (25) | 1618 (23) | 1623 (14) | 1617 (3) | 1601 (4) | 1587 (3) | 1588 (14) |
| $B_{\text {eq }}(\mathrm{Li})$ | $2 \cdot \dagger$ | $1 . \dagger$ | $1 \cdot 27$ (43) | 1.59 (15) | 1.18 (7) | 1.80 (10) | 2.31 (10) | $2 \cdot 90$ (5) |
| $B_{\text {eq }}(\mathrm{I})$ | 0.84 (2) | 0.5 | $0 \cdot 49$ (24) | 0.58 (5) | 0.43 (2) | 0.89 (3) | $1 \cdot 19$ (2) | 1.13 (3) |
| $B_{\text {eq }}(\mathrm{O})$ | 1.29 (28) | 1.02 | $1 \cdot 11$ (21) | 1.25 (5) | 0.96 (4) | 1.54 (5) | 2.01 (5) | 1.71 (5) |

Table 2. Experimental conditions for the measurement of thermal expansion of $\alpha-\mathrm{LiIO}_{3}$ (see Fig. 1)

| Sample | Instrument | Wavelength <br> $(\AA)$ | Symbol in <br> Fig. 1 |
| :--- | :---: | :---: | :---: |
| Powder 1 | Neutron D1A | 1.3885 | $O$ |
| Powder 2 | Neutron D1A | 1.9066 | $\square$ |
| Powder 3 | Neutron D1A | 1.9066 | $\times$ |
| Powder 4 | Neutron D1B | 2.524 | + |
| Crystal 1 | Neutron D9 | 0.5499 | $\square$ |
| Crystal 2 | X-ray PW1100 | 0.7107 | $\Delta$ |
| Crystal 3 | X-ray PW1100 | 0.7107 | $\odot$ |
| Crystal 4 | X-ray PW1100 | 0.7107 | $\Delta$ |
| Crystal 5 | X-ray PW1100 | 0.7107 | $\nabla$ |

## Thermal expansion

Cell parameters of $\alpha-\mathrm{LiIO}_{3}$ have been measured at various temperatures on different samples (powders, single crystals) and with different diffractometers and wavelengths (X-rays and neutrons). The experimental conditions are summarized in Table 2. Variations of $a$, $c$ and $c / a$ versus temperature are plotted in Fig. 1. For each measurement, the unit-cell constants were obtained by least-squares refinement; these cell parameters were subsequently fitted to the polynomials:

$$
\begin{aligned}
& a(T)=5.4771(11)+1.54(7) \times 10^{-4} T \quad(T \text { in } K) \\
& c(T)=5.1642(10)+2.81(3) \times 10^{-4} T .
\end{aligned}
$$

These polynomials fit the observations to better than two standard deviations. The thermal-expansion coefficients calculated as

$$
\alpha_{a}(T)=\frac{1}{a(T)}\left(\frac{\mathrm{d} a}{\mathrm{~d} T}\right)_{T}
$$

are, at 273 K : $\alpha_{a}=2.81(13) \times 10^{-5}$ and $\alpha_{c}=$ $5.44(5) \times 10^{-5} \mathrm{~K}^{-1}$, in fair agreement with previous measurements (Haussühl, 1970; Thierry, Coquet \& Crettez, 1976). Most of these data have been obtained from diffraction experiments aimed at the study of the


Fig. 1. $\alpha$ - $\mathrm{LiIO}_{3}$ cell constants versus temperature. See Table 2 for explanation of different signs. The solid lines are least-squares fits to the data.
$\alpha \neq \gamma$ phase transition; in this respect it is worth mentioning that this transition, which usually occurs at about 493 K in powdered samples, has never been observed for needle-shaped crystals even at temperatures as high as 533 K ; such crystals transform directly into the $\beta$ phase through a destructive transition.

## Discussion

The anisotropic thermal parameters obtained in the structure refinements are given in Table 3. It is worth noting that the anisotropy of the Li thermal parameters does not increase drastically as a function of temperature as might be expected from the strong increase of the ionic conductivity along the $\mathbf{c}$ direction (Remoissenet, Garandet \& Arend, 1975). This is actually in agreement with the powder NMR data (Durand-Le Floch, 1982) which unambiguously show:

- the presence of a single kind of Li atom with axial symmetry;
- no change of the electric-field gradient at the Li site between RT and 473 K ;
- no motional narrowing of the ${ }^{7} \mathrm{Li}$ NMR line in the same temperature range.
The thermal motion of I is almost isotropic, that of the O atom is slightly anisotropic. As expected the shortest axis of the ellipsoid (Fig. 2) lies along the direction of the shortest bond (r.m.s. displacement $0.081 \AA$ along $\mathrm{I}-\mathrm{O}$ at RT) whereas the longest axis ( $0 \cdot 129 \AA$ at RT) is perpendicular to the $\mathrm{I}-\mathrm{O}-$ Li plane.

The coordination environment of the Li atoms is a slightly elongated octahedron. Each $\mathrm{LiO}_{6}$ octahedron shares two opposite faces with two neighbouring octahedra and the resulting arrangement is an infinite string of $\mathrm{LiO}_{6}$ octahedra extending along the c direction

Table 3. $\alpha-\mathrm{LiIO}_{3}$ : anisotropic thermal parameters ( $\times 10^{4} \AA^{2}$ ) and $R$ factors

Symmetry restrictions are $U_{11}=U_{22}=2 U_{12}$ and $U_{13}=U_{23}=0$ for $I$ and Li atoms. $R$ factors quoted in this table refer to the positional parameters given in Table 1.

| Method* | $N P$ | $N$ | $N$ | $N$ | $X$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $T$ (K) | RT | RT | 373 | 475 | 525 |
| $\lambda(\AA)$ | 1.3885 | 0.5499 | 0.5499 | 0.5499 | 0.7107 |
| $U_{11}(\mathrm{Li})$ | 236 (15) | 155 (6) | 223 (10) | 309 (10) | 367 (68) $\dagger$ |
| $U_{33}(\mathrm{Li})$ | 135 (26) | 140 (13) | 237 (21) | 260 (17) |  |
| $U_{11}$ (I) | 102 (5) | 58 (2) | 118 (3) | 157 (2) | 151 (1) |
| $U_{33}(\mathrm{I})$ | 19 (7) | 49 (3) | 102 (4) | 140 (3) | 132 (2) |
| $U_{11}(\mathrm{O})$ | 124 (4) | 79 (2) | 146 (3) | 192 (3) | 140 (12) |
| $U_{22}(\mathrm{O})$ | 160 (4) | 146 (3) | 234 (4) | 295 (4) | 305 (20) |
| $U_{33}(\mathrm{O})$ | 152 (5) | 132 (3) | 204 (4) | 259 (3) | 219 (19) |
| $U_{12}(\mathrm{O})$ | 40 (4) | 50 (2) | 90 (3) | 108 (3) | 67 (12) |
| $U_{13}(\mathrm{O})$ | 35 (7) | 23 (2) | 33 (3) | 38 (3) | 75 (17) |
| $U_{23}(\mathrm{O})$ | 26 (5) | -7(2) | -9(4) | -12 (3) | -34 (22) |
| $R$ (\%) | 4.80 | $5 \cdot 36$ | 6.58 | $5 \cdot 13$ | $2 \cdot 64$ |

[^1]

Fig. 2. Stereoscopic drawing (ORTEP, Johnson, 1965) of an $a-\mathrm{LiIO}_{3}$ unit cell.


Fig. 3. Stereoscopic drawing (ORTEP) of the Li environment in $a-\mathrm{LiIO}_{3}$.
(Fig. 3). The $\mathrm{Li}^{+}$ion is slightly off-centred along the same direction which leads to two $\mathrm{Li}-\mathrm{O}$ distances (Table 4) but the average distance ( $2 \cdot 12 \AA$ at RT) is exactly that expected from the ionic radii (Shannon, 1976).

Each I atom is strongly bonded to three O atoms at a distance $d_{1}=1.803$ (1) $\AA$ to form a regular trigonal pyramid (Fig. 4) with $\mathrm{O}-\mathrm{O}$ distance $a_{1}=2.767$ (1) $\AA$ ( $\mathscr{C}$ configuration according to Brown, 1974). This pyramid is rigid and its shape and dimensions are almost temperature independent. The only effect of a temperature change is a rotation of the $\mathrm{IO}_{3}^{-}$pyramid around its threefold axis resulting in a variation of the angle $\theta_{1}$ between the projection of the $\mathrm{Li}-\mathrm{O}$ and $\mathrm{I}-\mathrm{O}$ bonds on the $x y$ plane (see Fig. 5 and Table 5). The I atom is also linked to three other O atoms at a distance $d_{2}=2.908$ (1) $\AA$ at room temperature; the triangle formed by these three O atoms does not rotate as a function of temperature but the distance $d_{2}$ has a rather large temperature dependence (Table 5).
The thermal expansion can be well accounted for by a combination of (1) the rotation of the rigid $\mathrm{IO}_{3}^{-}$group which contributes to nearly half of the $\alpha_{a}$ value and (2) the homothetic expansion of the $\mathrm{LiO}_{6}$ which contributes to the other half of $\alpha_{a}$ and accounts for the total expansion along c (see Fig. 4 and numerical values in Table 4). In this connection, it is worth mentioning that the thermal expansion of the $\mathrm{Li}-\mathrm{O}$ distance $\left[\alpha(\mathrm{Li}-\mathrm{O})=3.6 \times 10^{-5} \mathrm{~K}^{-1}\right]$ is almost twice the value

Table 4. Interatomic distances $(\AA)$, angles $\left({ }^{\circ}\right)$, and related thermal coefficients for the $\mathrm{LiO}_{6}$ octahedron in $\alpha-\mathrm{LiIO}_{3}$

|  | Short |  |  |  | Long |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T(\mathrm{~K})$ | $d_{1}(\mathrm{Li}-\mathrm{O})$ | $\varphi_{1}(\mathrm{O}-\mathrm{Li}-\mathrm{O})$ | $a_{1}(\mathrm{O}-\mathrm{O})=a_{2}$ |  | $d_{2}(\mathrm{Li}-\mathrm{O})$ | $\varphi_{2}(\mathrm{O}-\mathrm{Li}-\mathrm{O})$ |
| RT | $2.081(3)$ | $88.4(2)$ | $2.902(\mathrm{t})$ |  | $2.153(3)$ | $84.8(2)$ |
| 373 | $2.093(5)$ | $88.0(4)$ | $2.908(2)$ |  | $2.152(4)$ | $85.0(4)$ |
| 475 | $1.094(4)$ | $88.2(3)$ | $2.916(2)$ |  | $2.167(5)$ | $84.6(3)$ |
| $\alpha=\frac{1}{l} \frac{\mathrm{~d} l}{\mathrm{~d} T}$ | $3.6 \times 10^{-5}$ | $\frac{\overline{\mathrm{~d} \varphi_{1}}}{\mathrm{~d} T} \sim 0$ | $2.75 \times 10^{-5}$ | $3.7 \times 10^{-5}$ | $\frac{\mathrm{~d} \varphi_{2}}{\mathrm{~d} T} \sim 0$ |  |

Table 5. Interatomic distances $(\AA)$, angles $\left({ }^{\circ}\right)$ of position in the cell (see Fig. 5) and related thermal coefficients for the $\mathrm{IO}_{6}$ group in $\alpha-\mathrm{LiIO}_{3}$

|  | Short |  |  | Long |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T(\mathrm{~K})$ | $d_{1}(\mathrm{I}-\mathrm{O})$ | $a_{1}(\mathrm{O}-\mathrm{O})$ | $\theta_{1}$ | $d_{2}(\mathrm{I}-\mathrm{O})$ | $a_{2}(\mathrm{O}-\mathrm{O})$ | $\theta_{2}$ |
| RT | 1.803 (1) | 2.767 (1) | 15.16 (5) | 2.908 (1) | 4.024 (1) | 89.00 (5) |
| 373 | 1.801 (1) | 2.767 (2) | 14.96 (5) | 2.926 (2) | 4.042 (2) | 88.96 (5) |
| 475 | 1.801 (1) | 2.769 (1) | 14.70 (5) | 2.947 (1) | 4.068 (1) | 88.92 (5) |
| $\alpha=\frac{1}{l} \frac{\mathrm{~d} l}{\mathrm{~d} T}$ | $\sim 0$ | $\sim 0$ | $\frac{\mathrm{d} \theta_{1}}{\mathrm{~d} T}=-4.6 \times 10^{-s}$ | $7.7 \times 10^{-5}$ | $6.2 \times 10^{-3}$ | $\frac{\mathrm{d} \theta_{2}}{\mathrm{~d} T} \sim 0$ |



Fig. 4. Perspective drawing (ORTEP) of the $\mathrm{IO}_{6}$ octahedron.


Fig. 5. The $x y$-plane projection of the $\alpha-\mathrm{LiIO}_{3}$ unit cell.
quoted in the literature $\left[\alpha(\mathrm{Li}-\mathrm{O}) \sim 1.95 \times 10^{-5} \mathrm{~K}^{-1}\right.$ (Hazen \& Prewitt, 1977; Hazen \& Finger, 1981)]. However, this large value of the thermal expansion of the $\mathrm{Li}-\mathrm{O}$ distance can be qualitatively explained by the rather unusual arrangement of the $\mathrm{LiO}_{6}$ octahedra in the structure: indeed, the occurrence of infinite chains of face-sharing octahedra must lead to strong repulsive electrostatic interaction along the c direction, from which thermal expansion, larger than the values observed in the more usual corner-sharing structures, occurs.

## Lone pair

The crystal chemistry of $\mathrm{Sn}^{2+}, \mathrm{Sb}^{3+}, \mathrm{Te}^{4+}, \mathrm{I}^{5+}$ and $\mathrm{Xe}^{6+}$ oxides and fluorides has been rationalized by Brown (1974) and Galy, Meunier, Andersson \& Åström (1975) who have shown that the existence of lone-pair electrons in the valence shell requires a space comparable to that of an anion. This is clearly shown in Fig. 6 where I and $O$ atoms have been represented by spheres of radius equal to the usual crystal radii of $\mathrm{I}^{\text {s+ }}$ ( $0.44 \AA$ ) and $\mathrm{O}^{2-}(1.38 \AA)$. In their geometrical approach to the tetrahedral model (three anions + lone pair) Galy et al. (1975) assumed a quasi-regular environment of the lone-pair cation, i.e. they pictured the volume occupied by the lone-pair electrons as a sphere with the same radius as an O (or F ) atom. Analysis of a number of structures of iodates led us to the conclusion that this simplification overestimates the


Fig. 6. Projection on a plane parallel to $\mathbf{c}$ of the $\mathrm{IO}_{6}$ octahedron. Large circle: O, small circle: I, hatched circle: lone pair.

Table 6. Volume per anion (or anion + lone pair) for some iodate $\left(\mathrm{IO}_{3}+\right.$ lone pair) and periodate $\left(\mathrm{IO}_{4}\right)$ structures
$V_{1}=$ volume per anion (oxygen); $V_{2}=$ volume per (anion + lone pair).

Iodates: $I^{\mathbf{v}}$
Periodates: I $^{\text {VII }}$

| Compound | $V_{1}\left(\AA^{3}\right)$ | $V_{2}\left(\AA^{3}\right)$ | Compound | $V_{1}\left(\AA^{3}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{HIO}_{3}$ | 21.01 | 15.76 | $\mathrm{H}_{5} \mathrm{IO}_{6}$ | 18.71 |
| $\mathrm{HI}_{3} \mathrm{O}_{8}$ | 20.65 | 15.02 | $\mathrm{Li}_{3} \mathrm{IO}_{6}$ | 17.81 |
| $\alpha$ - $\mathrm{LiIO}_{3}$ | 22.42 | 16.81 | $\mathrm{Li}_{2} \mathrm{H}_{3} \mathrm{IO}$ | 18.76 |
| $\mathrm{CuIO}_{3} \mathrm{OH}$ | 21.69 | 17.35 | $\mathrm{LiIO}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ | 19.84 |
| $\beta-\mathrm{Ni}\left(\mathrm{IO}_{3}\right)_{2}$ | 21.59 | $16 \cdot 20$ | $\mathrm{MgH} \mathrm{IO}_{6} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ | 20.22 |
| $\mathrm{Co}\left(\mathrm{IO}_{3}\right)_{2}$ | 22.00 | 16.50 | $\mathrm{Al}\left(1 \mathrm{O}_{4}\right)_{3} \cdot 12 \mathrm{H}_{2} \mathrm{O}$ | 19.10 |
| $\alpha-\mathrm{Cu}\left(\mathrm{IO}_{3}\right)_{2}$ | 21.68 | 16.26 | $\mathrm{YIO}_{5} .4 \mathrm{H}_{2} \mathrm{O}$ | 19.87 |
| $\gamma-\mathrm{Cu}\left(\mathrm{IO}_{3}\right)_{2}$ | 21.47 | $16 \cdot 10$ | $\mathrm{GdIO}_{5} .4 \mathrm{H}_{2} \mathrm{O}$ | 20.18 |
| $\mathrm{Mn}\left(\mathrm{IO}_{3}\right)_{2}$ | 22.69 | 17.02 | $\mathrm{LuIO}_{5} .4 \mathrm{H}_{2} \mathrm{O}$ | 19.54 |
| $\mathrm{Al}\left(\mathrm{IO}_{3}\right)_{3}$ | 20.32 | $15 \cdot 24$ |  |  |
| $\mathrm{Cr}\left(\mathrm{IO}_{3}\right)_{3}$ | 20.73 | 15.54 | Average | 19.34 |
| $\mathrm{Fe}\left(\mathrm{IO}_{3}\right)_{3}$ | 21.39 | 16.04 |  |  |
| $\mathrm{Sc}\left(\mathrm{IO}_{3}\right)_{3}$ | 22.42 | 16.82 |  |  |
| $\mathrm{Y}\left(\mathrm{IO}_{3}\right)_{3}$ | 21.48 | $16 \cdot 11$ |  |  |
| $\mathrm{Gd}\left(\mathrm{IO}_{3}\right)_{3}$ | 22.35 | 16.76 |  |  |
| $\alpha-\mathrm{Lu}\left(\mathrm{IO}_{3}\right)_{3}$ | 21.08 | 15.81 |  |  |
| $\beta-\mathrm{Lu}\left(\mathrm{IO}_{3}\right)_{3}$ | 22.22 | 16.67 |  |  |
| $\mathrm{Zr}\left(\mathrm{IO}_{3}\right)_{4}$ | 21.82 | 16.37 |  |  |
| $\mathrm{Ce}\left(\mathrm{IO}_{3}\right)_{4}$ | 21.72 | 17.38 |  |  |
| $\mathrm{Ce}\left(\mathrm{IO}_{3}\right)_{4} \cdot \mathrm{H}_{2} \mathrm{O}$ | 21.77 | 16.65 |  |  |
| Average | 21.63 | $16 \cdot 32$ |  |  |

size of the lone pair. This can be seen for instance by comparing the volume per O for some iodate $\left(\mathrm{IO}_{3}+\right.$ lone pair) and periodate ( $\mathrm{IO}_{4}$ ) structures (Table 6); indeed the volume/anion is about $12 \%$ larger in iodates than in periodates (which shows that the lone pair is stereochemically active in iodates) but the average volume per (anion + lone pair) in iodates is $16 \%$ smaller than the average anionic volume in periodates. From these average volumes, one can estimate the radius of the I lone pair to be about $1 \AA$.
Therefore, in order to describe the structure of iodates, we propose modifying the tetrahedral model of Galy et al. (1975) in the following way: the $\mathrm{IO}_{3} \mathrm{~F}$
tetrahedron, where $E$ stands for lone pair, is no longer considered as regular and the radius of $E$ is allowed to be smaller than the radius of $O$. The result is a compressed $\mathrm{IO}_{3} E$ tetrahedron, having only one threefold axis, which can be described by three distances:

$$
\begin{aligned}
a_{1} & =\text { average } \mathrm{O}-\mathrm{O} \text { distance } \\
d_{1} & =\text { average } \mathrm{I}-\mathrm{O} \text { distance; } \\
\mathrm{I}-E & =\text { iodine-lone-pair distance. }
\end{aligned}
$$

This model is well suited to $\alpha$ - $\mathrm{LiIO}_{3}$ where the $\mathrm{IO}_{3}$ pyramid has $C_{3}$ symmetry but applies as well to other iodate structures (Coquet, 1982). The radius of the lone pair can then be simply evaluated from geometrical considerations, assuming a close packing of the lone pair and its six neighbouring O atoms (Fig. 4). Using our room-temperature structural results (Table 1) one finds for the lone pair a radius of $1.054 \AA$ in fair agreement with the above estimated value. The coordinates of $E$ are calculated as $x, y, z=0,0,0 \cdot 1947$, which gives $\mathrm{I}-E=1.007 \AA$, instead of $1.42 \AA$ in the regular tetrahedron model.

## Pyroelectric coefficient

The experimental pyroelectric coefficient $P_{3}$ has been found to be positive (Turner, 1976) and equal to about $10^{-5} \mathrm{C} \mathrm{m}^{-2} \mathrm{~K}^{-1}$ (Abrahams, 1978). This value can be well accounted for by a simple point-charge model including the lone pair. On the basis of such a model, the ionic contribution to the polarization $P_{s}$ may be evaluated as

$$
P_{s}=4 e \Delta z / a^{2} \sqrt{3}
$$

where $e$ is the elementary charge, $a$ the cell parameter of $\alpha-\mathrm{LiIO}_{3}$ and $\Delta z$ the distance along the $c$ axis between the position of the negative charge of $\left(\mathrm{IO}_{3} E\right)^{-}$and the nearest layer of $\mathrm{Li}^{+}$; the negative charge associated with the $\left(\mathrm{IO}_{3} E\right)^{-}$is taken to be at the centroid of the ionic distribution, every position being weighted by the magnitude of its formal charge (two for O and the lone pair, seven for I). This point-charge model yields a polarization parallel to $c$ of about $14.2 \times 10^{-2} \mathrm{C} \mathrm{m}^{-2}$ at room temperature and a pyroelectric coefficient $P_{3}$ (estimated from RT and 475 K data) of $0.34 \times 10^{-3}$ $\mathrm{Cm}^{-2} \mathrm{~K}^{-1}$ in rather fair agreement with the experimental value. It is worth noting that a similar model not including the lone pair gives a negative value $P_{3}=$ $-0.4 \times 10^{-5} \mathrm{C} \mathrm{m}^{-2} \mathrm{~K}^{-1}$.

In this connection one should mention that the displacement of the $\mathrm{Li}^{+}$ions relative to the $\left(\mathrm{IO}_{3} E\right)^{-}$ groups is $0.9 \times 10^{-4} \AA \mathrm{~K}^{-1}$ which compares well with the value of $0.4 \times 10^{-4} \AA \mathrm{~K}^{-1}$ estimated by Abrahams (1978), assuming zero thermal expansion.

Note added in proof: The authors wish to refer readers to a complementary study by Svensson, Albertsson, Liminga, Kvick \& Abrahams [J. Chem. Phys. (1983). 78, 7343-7352].

## References

Abrahams, S. C. (1978). Mater. Res. Bull. 13, 1253-1258.
Boer, J. L. de, van Bolhuis, F., Olthof-Hazekamp, R. \& Vos, A. (1966). Acta Cryst. 21, 841-843.

Brown, I. D. (1974). J. Solid State Chem. 11, 214-233.
Coppens, P., Leiserowitz, L. \& Rabinovich, D. (1965). Acta Cryst. 18, 1035-1038.
Coquet, E. (1982). Unpublished work.
Durand-Le Floch, M. (1982). Private communication.
Emiraliev, A., Kocharov, A. G., Yamzin, I. I. \& Lyubimtsev, V. A. (1976). Sov. Phys. Crystallogr. 21, 214.

Galy, J., Meunier, G., Andersson, S. \& Áström, A. (1975). J. Solid State Chem. 13, 142-159.
Haussühl, S. (1970). Acustica, 23, 165-169.
Hazen, R. M. \& Finger, L. W. (1981). In Structure and Bonding in Crystals, Vol. II, edited by M. O'Keefe \& A. Navrotsky. London: Academic Press.
hazen, R. M. \& Prewitt, C. T. (1977). Am. Mineral. 62, 309-315.
Hewat, A. W. (1973). Report AERE-R7350. AERE, Harwell, Oxfordshire.
Hewat, A. W. (1978). Powder preparation program. Institut Laue-Langevin.
Hewat, A. W. (1979). Acta Cryst. A35, 248.
International Tables for X-ray Crystallography (1974). Vol. IV. Birmingham: Kynoch Press.
Johnson, C. K. (1965). ORTEP. Report ORNL-3794. Oak Ridge National Laboratory, Tennessee.
Koester, L. \& Rauch, H. (1981). Summary of neutron scattering lengths. IAEA Contract 2517/RB.
Lehmann, M. S. \& Larsen, F. K. (1979). Acta Cryst. A30, 580-584.
Li, Y. Y. (1981). Ferroelectrics, 35, 167-172.
Remoissenet, M., Garandet, J. \& Arend, M. (1975). Mater. Res. Bull. 10, 181-185.
Rietveld, H. M. (1969). J. Appl. Cryst. 2, 65-71.
Rosenzweig, A. \& Morosin, B. (1966). Acta Cryst. 20, 758-761.
Shannon, R. D. (1976). Acta Cryst. A 32, 751-767.
Sheldrick, G. M. (1976). SHELX. A program for crystal structure determination. Univ. of Cambridge, England.
Thierry, J. M., Coquet, E. \& Crettez, J. M. (1976). Opt. Commun. 16, 417-419.
Turner, E. H. (1976). J. Appl. Cryst. 9, 52.


[^0]:    * Lists of observed and calculated structure factors at room temperature, 373,475 and 525 K for a single crystal and those for powder at room temperature have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 38426 ( 16 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH 1 2HU, England.

[^1]:    * $X$ : X-ray, single-crystal; $N$ : neutron, single-crystal; $N P$ : neutron, powder.
    $\dagger$ Isotropic thermal parameter.

